By Brook Valley Calculation Progression
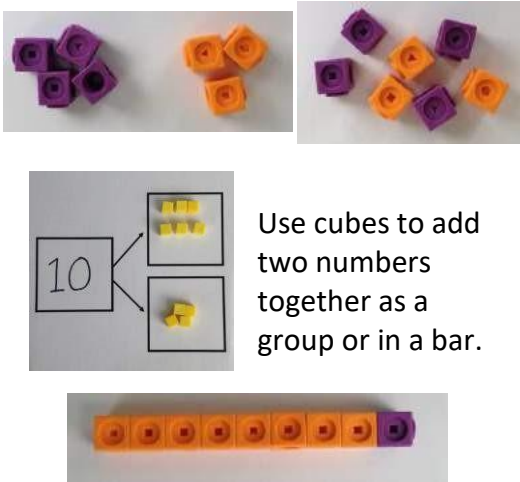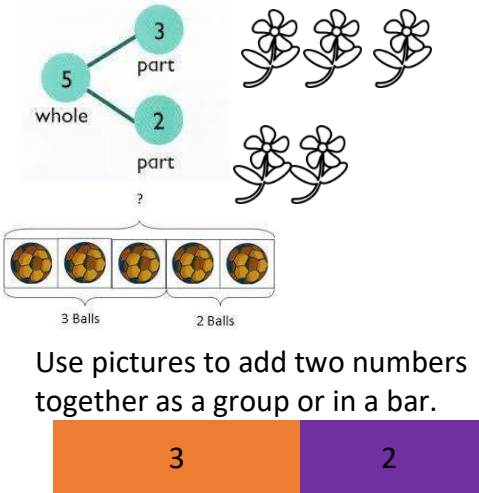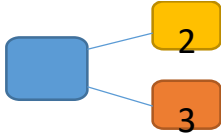
Intent: At By Brook Valley School we believe having a **clear progression of concrete, pictorial and abstract sequences** in our teaching the children will be able to **make links and build on previous learning** providing a **clear and consistent approach** to teaching calculation across the school. By embedding mathematical confidence through speaking in full mathematical sentences and using the correct vocabulary this will enable children to **secure and deepen their mathematical understanding** as they progress through the school.

Implementation: At By Brook Valley School we **use the White Rose maths medium term plans** to underpin our maths planning throughout the year which provides consistency and continuity across the school. However, **we adapt the teaching sequences** to the needs of our children and individual class delivery. The **White Rose maths block plans provide a scaffold for the teaching sequence** which follows the set calculation methods mapped out by White Rose but we heavily **support and adapt our teaching** with materials like the NCETM Progression Maps for Reasoning and Teaching for Mastery. In our school planning a teaching sequence in mathematics guidance there is a list of materials which we use to **support our teaching** to enable the children as mathematicians to **notice, describe, explain and make connections in their learning.**
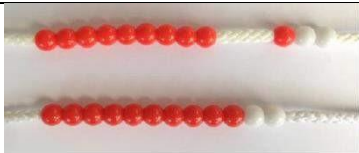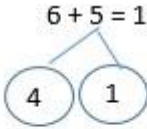
Impact: At By Brook Valley School the children will be familiar with a variety of representations in their calculation methods and be **confident to select** and draw upon the calculation method(s) they find most purposeful to describe, explain, compare and evaluate. They will be skilled in their level of understanding to **use mathematical vocabulary** and **sentence stems to explain** their mathematical understanding, sometimes with **multiple representations to compare and evaluate** efficiency and reliability and be able to make links and relationships interchangeably.
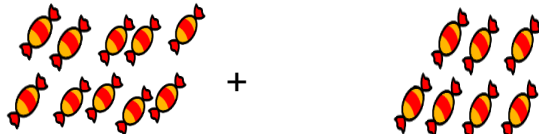
CALCULATION GUIDANCE: Addition

	Objective	Concrete	Pictorial	Abstract
EYFS	Counting a set of objects Knowing 1 more or 1 less Place numbers in order of size	Counting 1 more by manipulating objects and ordering size.	Counting using images and pictures.	Using more abstract images and numbers to count and order.
Year 1	Number bonds of 5, 6, 7, 8, 9 and 10	Use cubes to add two numbers together as a group or in a bar.	Use pictures to add two numbers together as a group or in a bar.	2 + 3 = 5 3 + 2 = 5 5 = 3 + 2 5 = 2 + 3 Use the part –part whole shown above

CALCULATION GUIDANCE: Addition

Counting	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	Use a number line to count on in ones.	5 + 3 = 8

	Objective	Concrete	Pictorial	Abstract
Year 1	Regrouping to make 10	6 + 5 = 11 Start with the bigger number and use the smaller number to make 10.	6 + 5 = 11 6 + 4 = 10 10 + 1 = 11	6 + 5 = 11

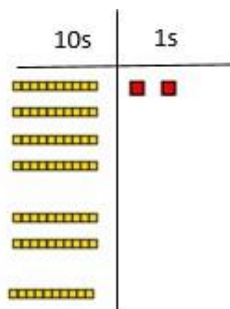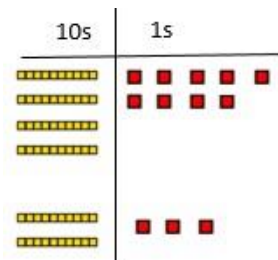# CALCULATION GUIDANCE: Addition

Year 2	Adding 3 single digit numbers	4 + 7 + 6= 17 Put 4 and 6 together to make 10. Add on 7. Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.	 Add together three groups of objects. Draw a picture to recombine the groups to make 10. 	$4 + 7 + 6 = \boxed{10} + \boxed{7}$ 10 $= \boxed{17}$ Combine the two numbers that make 10 and then add on the remainder.

	Objective	**Concrete**	**Pictorial**	**Abstract**
Year 2	Column method without regrouping	Add together the ones first, then add the tens. Use the Base 10 blocks first before moving onto place value counters. 24 + 15 = 44 + 15 =	After physically using the base 10 blocks and place value counters, children can draw the counters to help them to solve additions. 	24 + 15 = 39 24 + 15 39

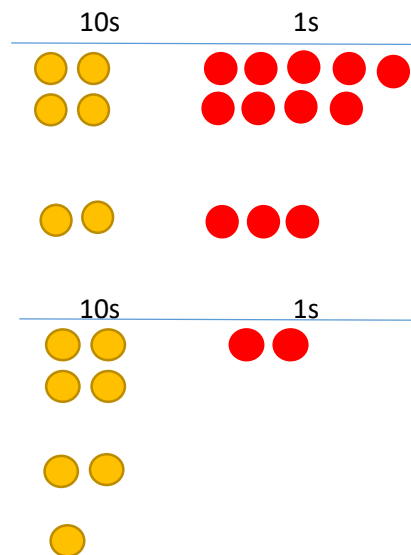# CALCULATION GUIDANCE: Addition

Make both numbers on a place value grid.

10s | 1s

Add up the units and exchange 10 ones for 1 ten.

Using place value counters, children can draw the counters to help them to solve additions.

10s | 1s
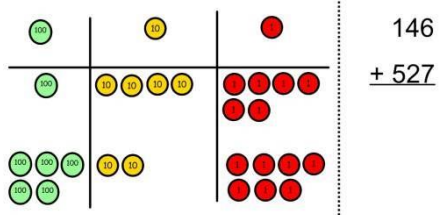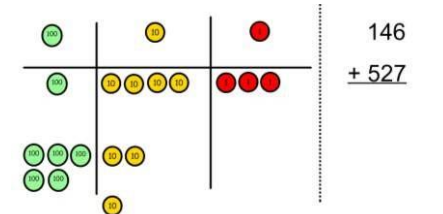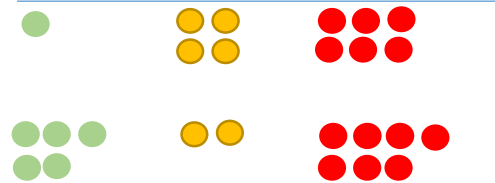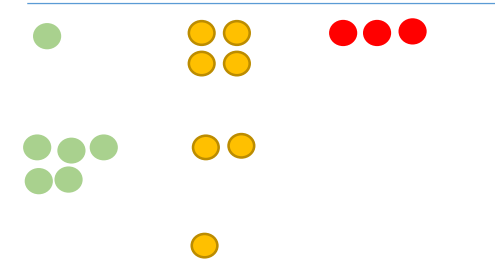
10s | 1s
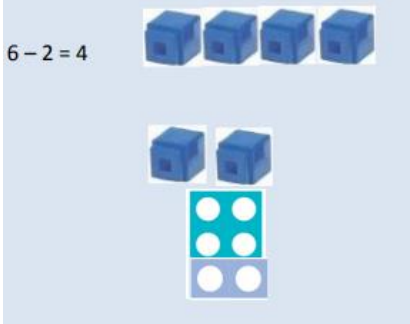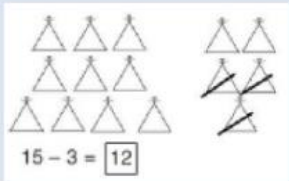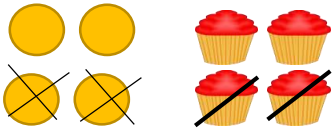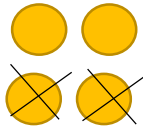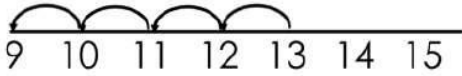
40 + 9
20 + 3
60 + 12 = 72

CALCULATION GUIDANCE: Addition

|	Objective	Concrete	Pictorial	Abstract
Year 3/4	Column method with regrouping	Make both numbers on a place value grid. 146 + 527 Add up the units and exchange 10 ones for 1 ten. 146 + 527 As children move on to decimals, money and decimal place value counters can be used to support learning. **NB** By Year 4 children will progress on to adding four digit numbers.	100s 10s 1s 100s 10s 1s Children can draw a pictorial representation of the columns and place value counters to further support their learning and understanding. **NB** Addition of money needs to have £ and p added separately.	100 + 40 + 6 <u>500 + 20 + 7</u> 600 + 70 + 3 = 673 As the children progress, they will move from the expanded to the compacted method. 146 + <u>527</u> 673 1 As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here.
Year 5/6	Column method with regrouping	Consolidate understanding using numbers with more than 4 digits and extend by adding numbers with up to 3 decimal places.		

CALCULATION GUIDANCE: Subtraction

|	Objective	Concrete	Pictorial	Abstract
EYFS	One less than/taking away ones	Use physical objects, counters, cubes numicon, etc, to show how objects can be taken away. 6 – 2 = 4	Cross out drawn objects to show what has been taken away. 15 – 3 = 12 4 – 2 = 2	18 – 3 = 15 8 – 2 = 6 Although number sentences are recorded in the concrete and pictorial methods children are introduced to them on their own while encouraging them to mentally take away ones.
Year 1	Taking away ones	Use physical objects, counters, cubes etc. to show how objects can be taken away. 4 – 2 = 2	Cross out drawn objects to show what has been taken away. 4 – 2 = 2	4 – 2 = 2
Year 1	Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. 13 – 4 = 9	Count back on a number line or number track 9 10 11 12 13 14 15 Start at the bigger number and count back the smaller number, showing the jumps on the number line.	Put 13 in your head, count back 4. What number are you at? Use your fingers to help.

CALCULATION GUIDANCE: Subtraction

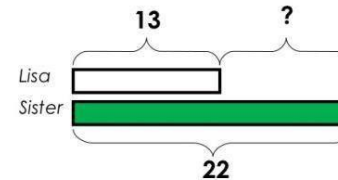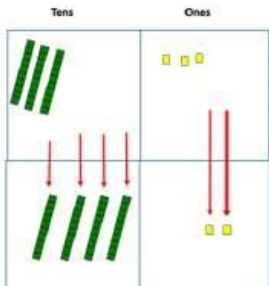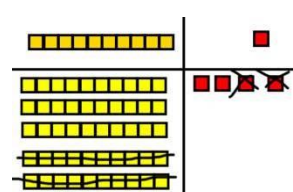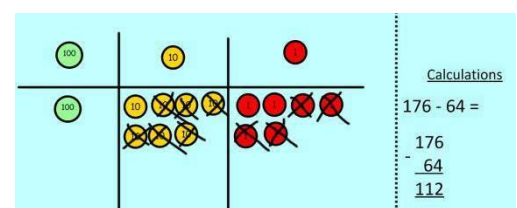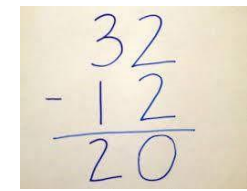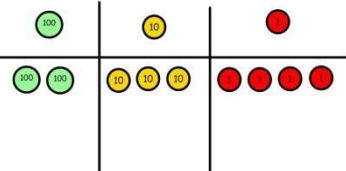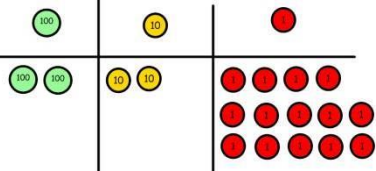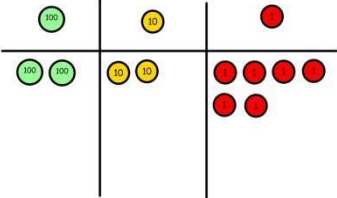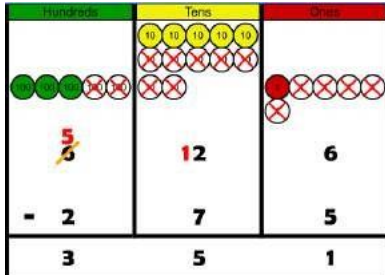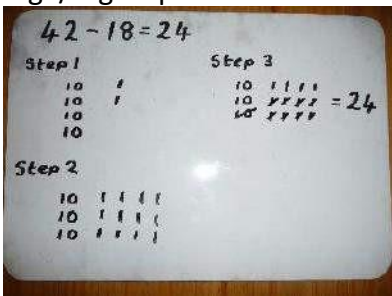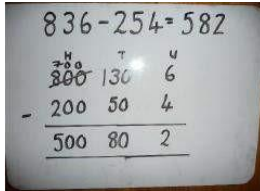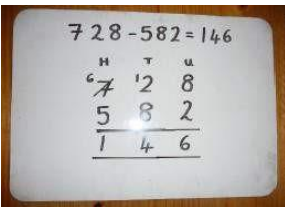| Find the difference | Compare amounts and objects to find the difference.

8 goldfish

3 goldfish ?
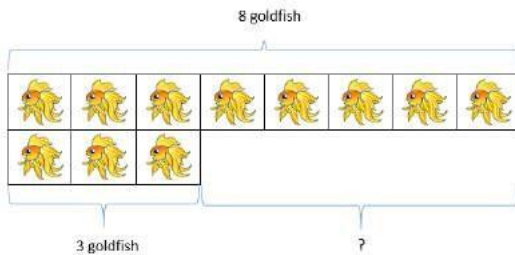
Use cubes to build towers or make bars to find the difference. Use basic bar models with items to find the difference. | + 5

0 1 2 3 4 5 6 7 8 9 10
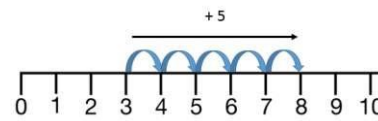
Count on to find the difference.

Lisa is 13 years old. Her sister is 22 years old. Find the difference in age between them.

13   ?
Lisa
Sister
22

Draw bars to find the difference between 2 numbers. | Hannah has 8 goldfish.
Helen has 3 goldfish.
Find the difference between the number of goldfish the girls have. |

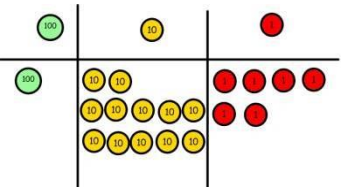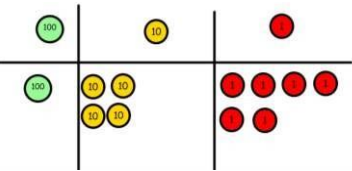# CALCULATION GUIDANCE: Subtraction

	Objective	Concrete	Pictorial	Abstract
Year 2	Column method without regrouping	75 − 42 = 33 Use Base 10 to make the bigger number then take the smaller number away. Show how you partition numbers to subtract. Again make the larger number first.	Draw the Base 10 or place value counters alongside the written calculation to help to show working.	This will lead to a clear written column subtraction.
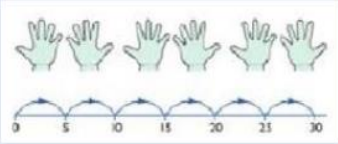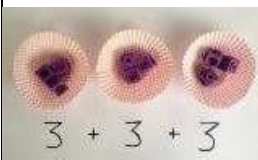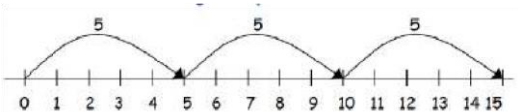
CALCULATION GUIDANCE: Subtraction

	Objective	Concrete	Pictorial	Abstract
Year 3 onwards	Column method with regrouping	Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges. Make the larger number with the place value counters 234 - 88 Start with the ones, can I take away 8 from 4 easily? I need to exchange 1 of my tens for 10 ones. 234 - 88 Now I can subtract my ones. 234 - 88	 Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make. When confident, children can find their own way to record the exchange/regrouping. Just writing the numbers as shown here shows that the child understands the method and knows when to exchange/regroup. 	 Children can start their formal written method by partitioning the number into clear place value columns. Moving forward the children use a more compact method. This will lead to an understanding of subtracting any number including decimals.
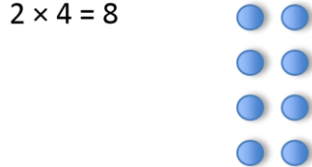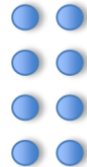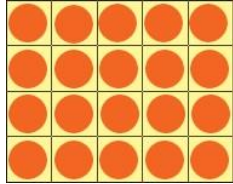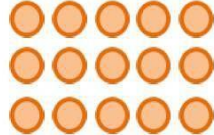
CALCULATION GUIDANCE: Subtraction

	Objective	Concrete	Pictorial	Abstract
Year 3 up	Column method with regrouping	Now look at the tens, can I take away 8 tens easily? I need to exchange 1 hundred for 10 tens. Calculations 234 - 88 Now I can take away 8 tens and complete my subtraction. Calculations 234 - 88 146 Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.		

CALCULATION GUIDANCE: Multiplication

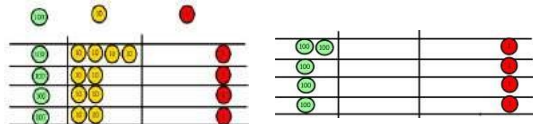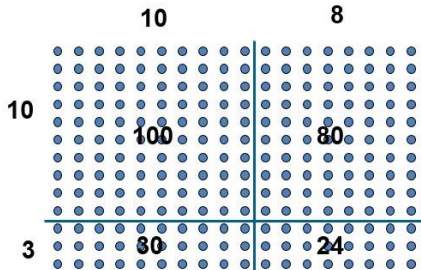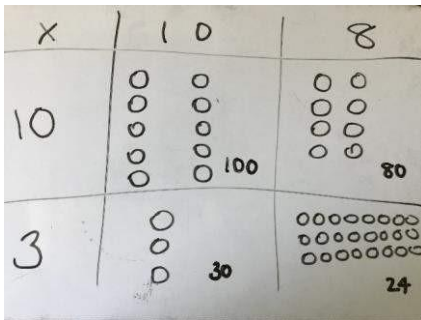|	Objective	Concrete	Pictorial	Abstract
EYFS	Doubling/counting in multiples	Use practical activities to show how to double a number. Count in multiples supported by concrete objects in equal groups.	Draw pictures to show how to double a number. Use a number line or pictures to continue support in counting in multiples.	Count out loud in multiples of a number. Write sequences with multiples of numbers.
Year 1/2	Repeated addition	Use different objects to add equal groups.	There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there? 2 + 2 + 2 = 6 5 + 5 + 5 = 15	Write addition sentences to describe objects and pictures. 2 + 2 + 2 = 6

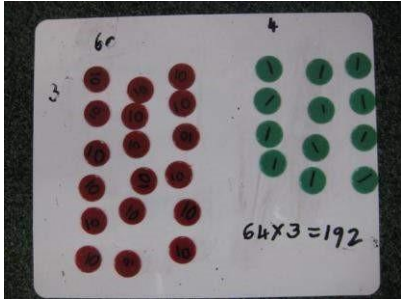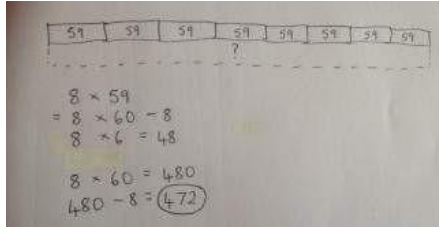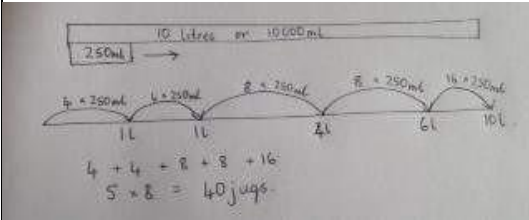|			
Arrays- showing commutative multiplication	Create arrays using counters/cubes to show multiplication sentences. 	Draw arrays in different rotations to find **commutative** multiplication sentences. $4 \times 2 = 8$ $2 \times 4 = 8$ $2 \times 4 = 8$ $4 \times 2 = 8$ Link arrays to area of rectangles. 	Use an array to write multiplication sentences and reinforce repeated addition. $5 + 5 + 5 = 15$ $3 + 3 + 3 + 3 + 3 = 15$ $5 \times 3 = 15$ $3 \times 5 = 15$

CALCULATION GUIDANCE: Multiplication

	Objective	Concrete	Pictorial	Abstract
Year 3/4	Grid method	Show the link with arrays to first introduce the grid method. 4 rows of 10 4 rows of 3 Move on to using Base 10 to move towards a more compact method. 4 rows of 13 Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows. Calculations 4 x 126 Fill each row with 126. Calculations 4 x 126 Add up each column, starting with the ones making any exchanges needed.	Children can represent the work they have done with place value counters in a way that they understand. They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below. 24 X 3 = 72	Start with multiplying by one digit numbers and showing the clear addition alongside the grid. | ×	30	5
7	210	35 | 210 + 35 = 245 Moving forward, multiply by a 2 digit number showing the different rows within the grid method. 10 / 8 10 / 100 / 80 3 / 30 / 24 | X	1000	300	40	2
10	10000	3000	400	20
8	8000	2400	320	16	
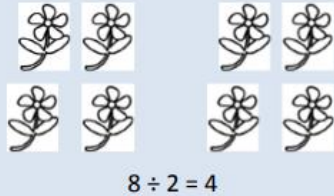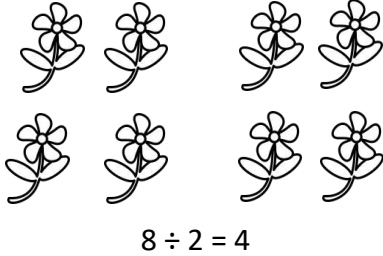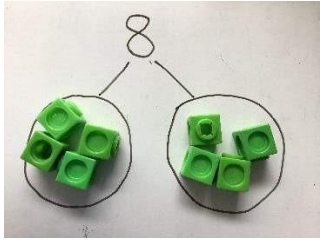
4 × 126 = 504

	Objective	Concrete	Pictorial	Abstract
	Expanded method	Show the link with arrays to first introduce the expanded method.		Start with long multiplication, reminding the children about lining up their numbers clearly in columns.
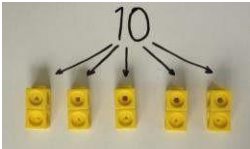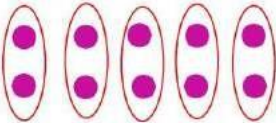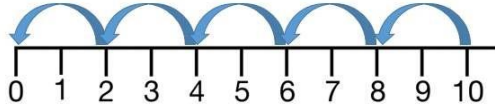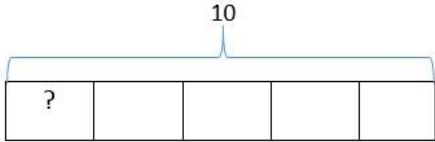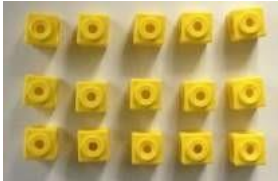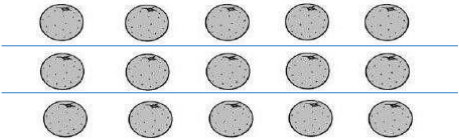
Year 5/6	Compact method	Children can continue to be supported by place value counters at the stage of multiplication. It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below.	Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.	Start with long multiplication, reminding the children about lining up their numbers clearly in columns. If it helps, children can write out what they are solving next to their answer. This moves to the more compact method.

CALCULATION GUIDANCE: Division
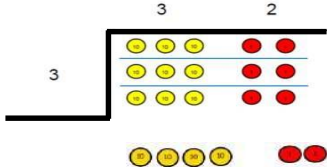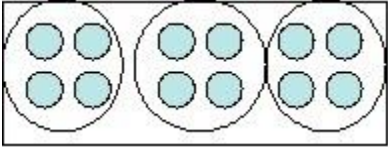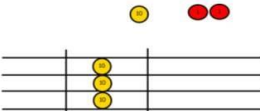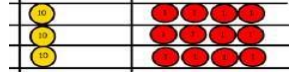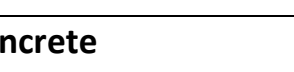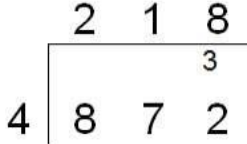
	Objective	Concrete	Pictorial	Abstract
EYFS	Sharing objects equally	I have 10 cubes; can you share them equally into 2 groups?	One sweet for you, one for me... Is it fair? How many do we each have?	Children use pictures or shapes to share quantities. $8 \div 2 = 4$
Year 1/2	Sharing	I have 8 cubes, can you share them equally between two people?	Children use pictures or shapes to share quantities. $8 \div 2 = 4$	Share 8 buns between two people. $8 \div 2 = 4$

CALCULATION GUIDANCE: Division
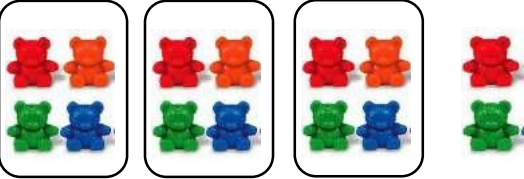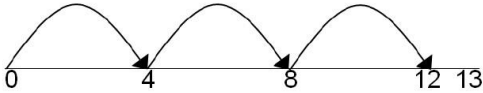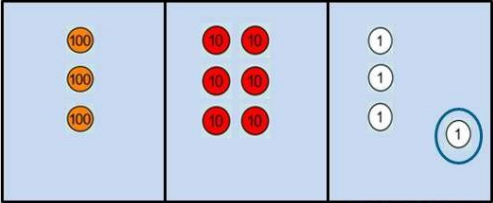
<table>
<tr>
<td rowspan="2">Grouping</td>
<td>Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.

</td>
<td>Use a number line to show jumps in groups. The number of jumps equals the number of groups.

Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.

$10 \div 5 = ?$

$5 \times ? = 10$</td>
<td>$10 \div 5 = 2$

Divide 10 into 5 groups. How many are in each group?</td>
</tr>
</table>

	Objective	Concrete	Pictorial	Abstract
Year 3/4	Division with arrays	Link division to multiplication by creating an array and thinking about the number sentences that can be created. Eg $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$	Draw an array use lines to split the array into groups to make multiplication and division	Find the inverse of multiplication and division sentences by creating four linking number sentences. $5 \times 3 = 15$ $3 \times 5 = 15$ $15 \div 5 = 3$ $15 \div 3 = 5$

CALCULATION GUIDANCE: Division

	Objective	Concrete	Pictorial	Abstract
	Short division	Use place value counters to divide using the short division method alongside. 96 ÷ 3 42 ÷ 3 Start with the biggest place value We are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over. We exchange this ten for 10 ones and then share the ones equally among the groups. We look at how many are in each group.	Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups. Encourage them to move towards counting in multiples to divide more efficiently.	Begin with divisions that divide equally with no remainder. 2 1 8 3 4	8 7 2

Note: the Objective/Concrete/Pictorial/Abstract labels appear as the bottom header row of the table.

CALCULATION GUIDANCE: Division

<table>
<tr>
<td rowspan="2">Year 5/6</td>
<td>Division with remainders</td>
<td>14 ÷ 3 =
Divide objects between groups and see how much is left over
</td>
<td>Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.

Draw dots and group them to divide an amount and clearly show a remainder.
</td>
<td>Complete written divisions and show the remainder using r.

29 ÷ 8 = 3 REMAINDER 5
↑ ↑ ↑   ↑
dividend divisor quotient   remainder</td>
</tr>
<tr>
<td>Short division with remainders</td>
<td>364 ÷ 3 =

1 2 1 rem 1
3 | 3 6 4
</td>
<td></td>
<td>Move onto divisions with a remainder. Once children understand remainders, begin to express as a fraction or decimal according to the context.

8 6 r 2
3
5 | 4 3 2

1 8 6 1/5
5 | 9 ^{4}3 ^{3}1

1 4 . 6
16   21
3 5 | 5 1 1 . 0</td>
</tr>
</table>

	Objective	Concrete	Pictorial	Abstract

CALCULATION GUIDANCE: Division

Year 6	Long division			Children will use long division to divide numbers with up to 4 digits by 2 digit numbers.
				$$\begin{array}{r} 015 \\ 32{\overline{\smash{)}487}} \\ -0 \\ \hline 48 \\ -32 \\ \hline 167 \\ -160 \\ \hline 7 \end{array}$$
				$$\begin{array}{r} 17 \text{ r } 19 \\ 31{\overline{\smash{)}546}} \\ 31\downarrow \\ \hline 236 \\ 217 \\ \hline 19 \end{array}$$